

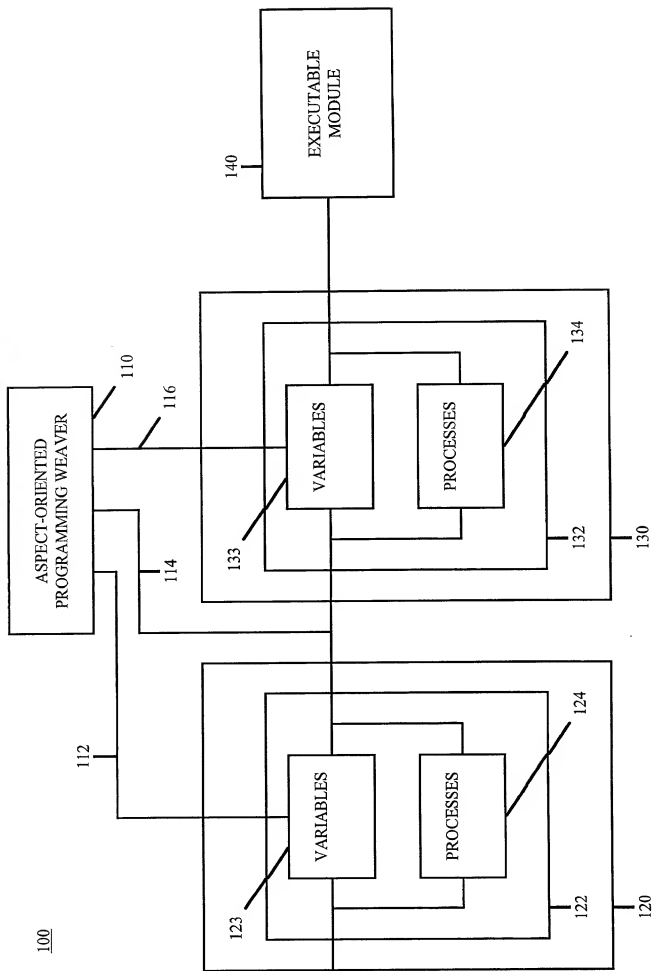
100

FIG. 1

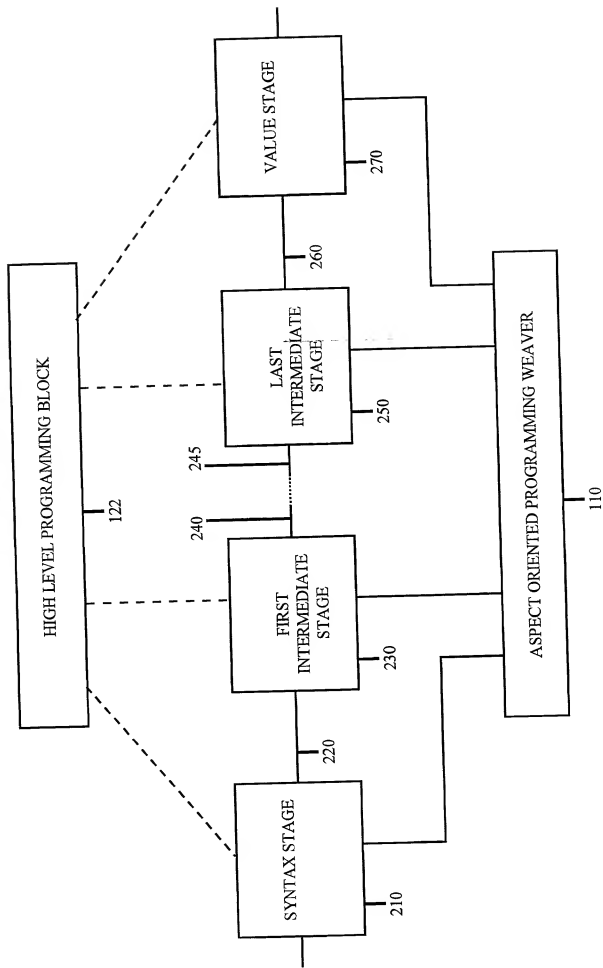


FIG. 2

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1  (stage requested-loops)
2  (projection key :defined-on requested-loops)
3  (projection computing-loop :defined-on requested-loops)
4  (define test
5    (lambda (x y z)
6      (and! (and! X y) z)))
7  (define and!
8    (reduction-stage requested-loops
9      (lambda (arg1 arg2)
10        (pointwise #'and arg1 arg2))))
11 (propagator requested-loops :bottom-up
12   (lambda (term)
13     (case requested-loops term
14       ((pointwise op arg1 arg2) (op arg1 arg2)
15        (let ((starting-loop
16              (fuse-loops (get-or-make-loop arg1) (get-or-make-loop arg2))
17                        (my-key (gensym))))
18          (deconstruct requested-loops starting-loop
19            (ptw-loop fn inputs outputs) (fn inputs outputs)
20            (let* ((new-fn (reduction-stage computation
21                          (lambda (args)
22                            (let* ((temp (fn args))
23                                   (result
24                                     (op (find (key arg1) temp)
25                                             (find (key arg2) temp))))
26                              (cons (cons my-key result)
27                                    temp))))
27              (new-loop (defer (ptw-loop new-fn inputs outputs))))
28            (update (key value) my-key)
29            (update (computing-loop value) new-loop))
30            (if (computing-loop arg1)
31              (update (computing-loop arg1)
32                (defer (loop-reference value))))
33            (if (computing-loop arg2)
34              (update (computing-loop arg2)
35                (defer (loop-reference value))))))
36       (else (note-demands value)
37         )))
38 )))
39

```

FIG. 3A

```

39 (define get-or-make-loop (value)
40   (if (and (same-frequency value) (computing-loop value))
41       (get-loop value)
42       (defer (ptw-loop
43               (reduction-stage computation
44                 (lambda (args) args)
45                 (list (cons (key value) value))
46                     nil))))))
47 (define get-loop
48   (reduction-stage computation
49     (lambda (value)
50       (computing-loop (get-loop-location value)))))
51 (define get-loop-location
52   (reduction-stage computation
53     (lambda (value)
54       (case requested-loops (computing-loop value)
55         ((loop-reference next) (next)
56          (get-loop-location next))
57         (else value))))))
58 (define note-demands (value)
59   (case requested-loops value
60     ((fn . args) (fn args)
61                  (record-demand fn)
62                  (map args #record-demand))
63     ((case stage value (pattern vars body) (else otherwise))
64      (stage value pattern vars body otherwise)
65      (record-demand value)
66      (record-demand body)
67      (record-demand otherwise))
68     ((lambda vars body) (vars body)
69      (record-demand body))))
70 (define record-demand (value)
71   (if (computing-loop value)
72       (let ((place (get-loop-location value))
73             (key (key value)))
74         (case requested-loops (computing-loop place)
75           ((ptw fn inputs outputs) (fn inputs outputs)
76            (if (not (member key outputs))
77                (let ((new-outputs (cons key outputs)))
78                  (update (computing-loop place)
79                          (delay (ptw fn inputs new-outputs))))))))))
80

```

FIG. 3B

```

80 (define ptw-loop
81   (lambda (fn inputs outputs)
82     (let ((output-pairs (early-mapcar (reduction-stage computation
83                                       (lambda (key) (cons key (new-array)))
84                                       outputs))))
85       (dotimes ((i 0 99))
86         (let* ((input-scalars
87                 (early-mapcar (reduction-stage computation
88                               (lambda (pair)
89                                 (let ((key (first pair))
40                                  (array (second pair)))
40                                  (cons key (elt array i)
41                                  inputs))
42                 (output-scalars (fn input-scalars)))
43       (early-map (reduction-stage computation
44                   (lambda (pair)
45                     (let ((key (first pair))
46                           (array (second pair)))
47                       (setf (elt array i)
48                             (find key output-scalars))))
49                   output-pairs))))))
100
101 (define pointwise (fn op1 op2 => result)
102   (reduction-stage computation ;; inlineable after loop fusion
103     (find (key result) (get-loop result))))
104
105 (define fuse-loops
106   (lambda (loop1 loop2)
107     (if (stage-eq requested-loops loop1 loop2)
108         loop1
109         (deconstruct loop-structure loop1
110           ((ptw-loop fn1 inputs1 outputs1) (fn1 inputs1 outputs1)
111            (deconstruct loop-structure loop2
112              ((ptw-loop fn2 inputs2 outputs2) (fn2 inputs2 outputs2)
113               (let ((inputs (merge inputs1 inputs2))
114                   (outputs (append outputs1 outputs2)))
115                 (ptw-loop
116                   (preserves computation
117                     (lambda (inputs) (merge (fn1 inputs) (fn2 inputs)))
118                   inputs outputs))))))))))
119
120 (define find
121   (reduction-stage computation ;; inlineable after loop fusion
122     (lambda (id list)
123       (deconstruct computation list
124         (cons (cons key value) rest) (key value rest)
125         (if (stage-eq computation key id)
126             value
127             (find id rest))))))
128
129 (define merge
130   ... like find

```

FIG. 3C

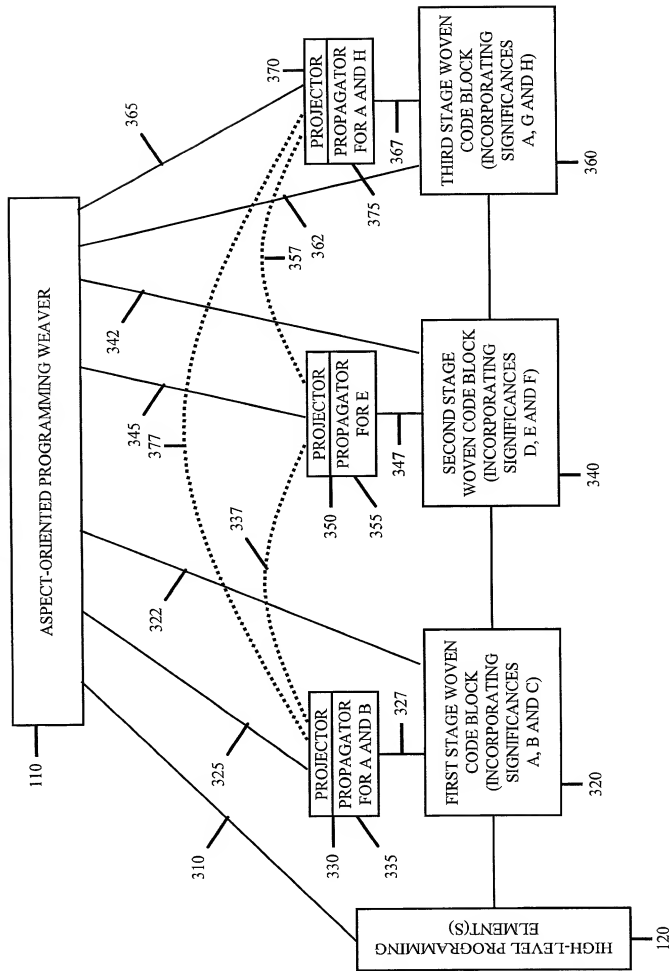


FIG. 4

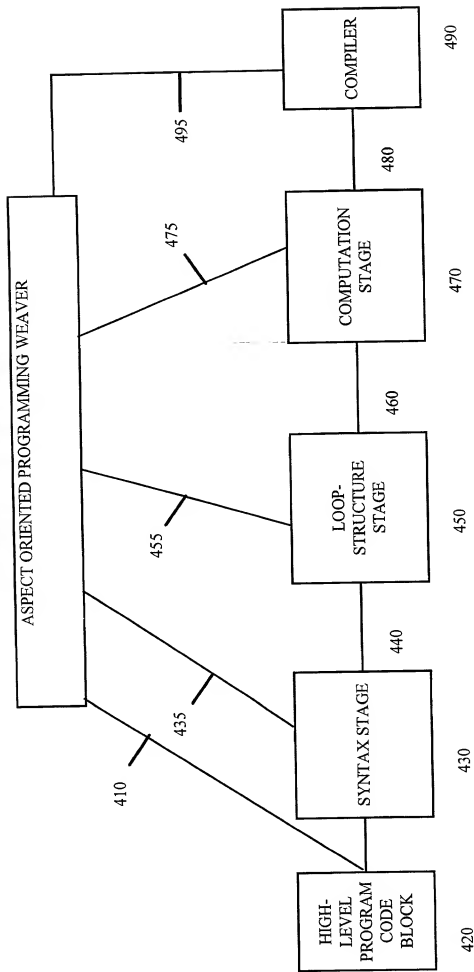


FIG. 5